Math 181 Quiz 3 Version A

1. Find all values of x which satisfy

(i)
$$x^3 \ge x$$

(ii)
$$|x-4| < 1$$
.

2. Use the ϵ - δ definition of continuity to show that $f(x) = \frac{1}{x}$ is continuous at $x_0 = 4$.

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3. Use the summation formulas

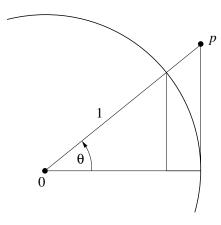
$$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}, \qquad \sum_{k=1}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}, \qquad \sum_{k=1}^{n} k^3 = \frac{n^2(n+1)^2}{4}$$

to find a formula for each of the following sums.

(i)
$$\sum_{k=3}^{n} (k^2 + 2k)$$

(ii)
$$\sum_{k=n}^{n+5} k$$

4. Consider the circle of radius one centered at the origin in the Cartesian plane and the two right triangles depicted below.



What are the coordinates of the point p in terms of the angle θ ?