Math 181 Honors Homework 7 Worksheet Version A

1. Use the limit definition of derivative to show the following:

(i) If
$$u(x) = \sqrt{g(x)}$$
 then $u'(x) = \frac{g'(x)}{2\sqrt{g(x)}}$.

(ii) If
$$v(x) = f(x^2)$$
 $v'(x) = f'(x^2)2x$.

(iii) If
$$w(x) = f(g(x))$$
 then $w'(x) = f'(g(x))g'(x)$.

2. Use the rules for differentiating functions to find the following derivatives:

(i) Find
$$f'(x)$$
 where $f(x) = 3x^4 + x^3 + x^2 + 17x - 5$.

(ii) Find
$$g'(x)$$
 where $g(x) = \frac{x^2 - 1}{x^2 + 1}$.

(iii) Find
$$u'(x)$$
 where $u(x) = \frac{1}{\sqrt{\sin(x)}}$.

(iv) Find
$$v'(x)$$
 where $v(x) = \cos(x^2)$.

(v) Find
$$w'(x)$$
 where $w(x) = \sin(x-1)\cos(x+1)$

- 3. Work problems 1, 2, 8 13 from Lang page 56.
- 4. Work problems 3, 5, 10 from Lang page 56.
- 5. Work problems 27, 38, 40, 44, 55, 56 from Ayres and Mendelson page 87.