## Math 181 Honors Quiz 3 Version A

1. Provided  $x \neq 1$ , then the sum  $x^3 + x^4 + \cdots + x^{12}$  is equal to

(A) 
$$\frac{x^{13} - x^3}{1 - x}$$
.

(B) 
$$\frac{x^{12} - x^3}{1 - x}$$
.

(C) 
$$\frac{x^{12} - x^4}{1 - x}$$
.

- (D) none of the above.
- 2. Prove the harmonic series  $\sum_{n=1}^{\infty} \frac{1}{n}$  diverges.

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- 3. Sum the series  $\sum_{n=2}^{\infty} \frac{1}{5^n}$ .
- 4. Prove one of the following theorems:

The Nested Interval Theorem. If  $I_1, I_2, I_3, \ldots$  is a sequence of closed intervals that are "nested," that is, each  $I_n$  contains  $I_{n+1}$ , then the intervals  $I_n$  have at least one point in common.

Convergence of the Alternating Harmonic Series. The alternating series  $\sum_{n=1}^{\infty} (-1)^{(n+1)} \frac{1}{n}$  converges.