

> #Compute the surface area of a chopped off cone.

> restart;

> eq1:=L=sqrt(w^2+(R-r)^2);

$$eq1 := L = \sqrt{w^2 + R^2 - 2 R r + r^2}$$

> eq2:=(2\*Pi-theta)\*rho=2\*Pi\*R;

$$eq2 := (2 \pi - \theta) \rho = 2 \pi R$$

> eq3:=(2\*Pi-theta)\*(rho-L)=2\*Pi\*r;

$$eq3 := (2 \pi - \theta) (\rho - L) = 2 \pi r$$

> A:=Pi\*rho^2-theta/2\*rho^2-(Pi\*(rho-L)^2-theta/2\*(rho-L)^2);

$$A := \pi \rho^2 - \frac{1}{2} \theta \rho^2 - \pi (\rho - L)^2 + \frac{1}{2} \theta (\rho - L)^2$$

> v:=solve({eq1,eq2,eq3},{rho,L,theta});

$$v := \left\{ \begin{array}{l} L = \sqrt{w^2 + R^2 - 2 R r + r^2}, \rho = \frac{\sqrt{w^2 + R^2 - 2 R r + r^2} R}{R - r}, \\ \theta = - \frac{2 \pi (-\sqrt{w^2 + R^2 - 2 R r + r^2} + R - r)}{\sqrt{w^2 + R^2 - 2 R r + r^2}} \end{array} \right\}$$

> A1:=subs(v,A);

$$A1 := \frac{\pi (w^2 + R^2 - 2 R r + r^2) R^2}{(R - r)^2} + \frac{\pi (-\sqrt{w^2 + R^2 - 2 R r + r^2} + R - r) \sqrt{w^2 + R^2 - 2 R r + r^2} R^2}{(R - r)^2} - \pi \left( \frac{\sqrt{w^2 + R^2 - 2 R r + r^2} R}{R - r} - \sqrt{w^2 + R^2 - 2 R r + r^2} \right)^2 - \frac{1}{\sqrt{w^2 + R^2 - 2 R r + r^2}} \left( \pi (-\sqrt{w^2 + R^2 - 2 R r + r^2} + R - r) \left( \frac{\sqrt{w^2 + R^2 - 2 R r + r^2} R}{R - r} - \sqrt{w^2 + R^2 - 2 R r + r^2} \right)^2 \right)$$

> simplify(A1);

$$\pi \sqrt{w^2 + R^2 - 2 R r + r^2} (R + r)$$

