

```
> restart;  
> f:=1/4+4*t^2*(1-t);  
> g:=1/4+sin(Pi*t);
```

$$f := \frac{1}{4} + 4t^2(1-t)$$

$$g := \frac{1}{4} + \sin(\pi t)$$

(1)

```
> df:=diff(f,t);  
> dg:=diff(g,t);
```

$$df := 8t(1-t) - 4t^2$$

$$dg := \cos(\pi t) \pi$$

(2)

```
> A:=int(dg*f,t=0..1);
```

$$A := \frac{4(-12 + \pi^2)}{\pi^3}$$

(3)

```
> Int(dg*f,t=0..1);
```

$$\int_0^1 \cos(\pi t) \pi \left(\frac{1}{4} + 4t^2(1-t) \right) dt$$

(4)

```
> evalf(A);
```

$$-0.2748341076$$

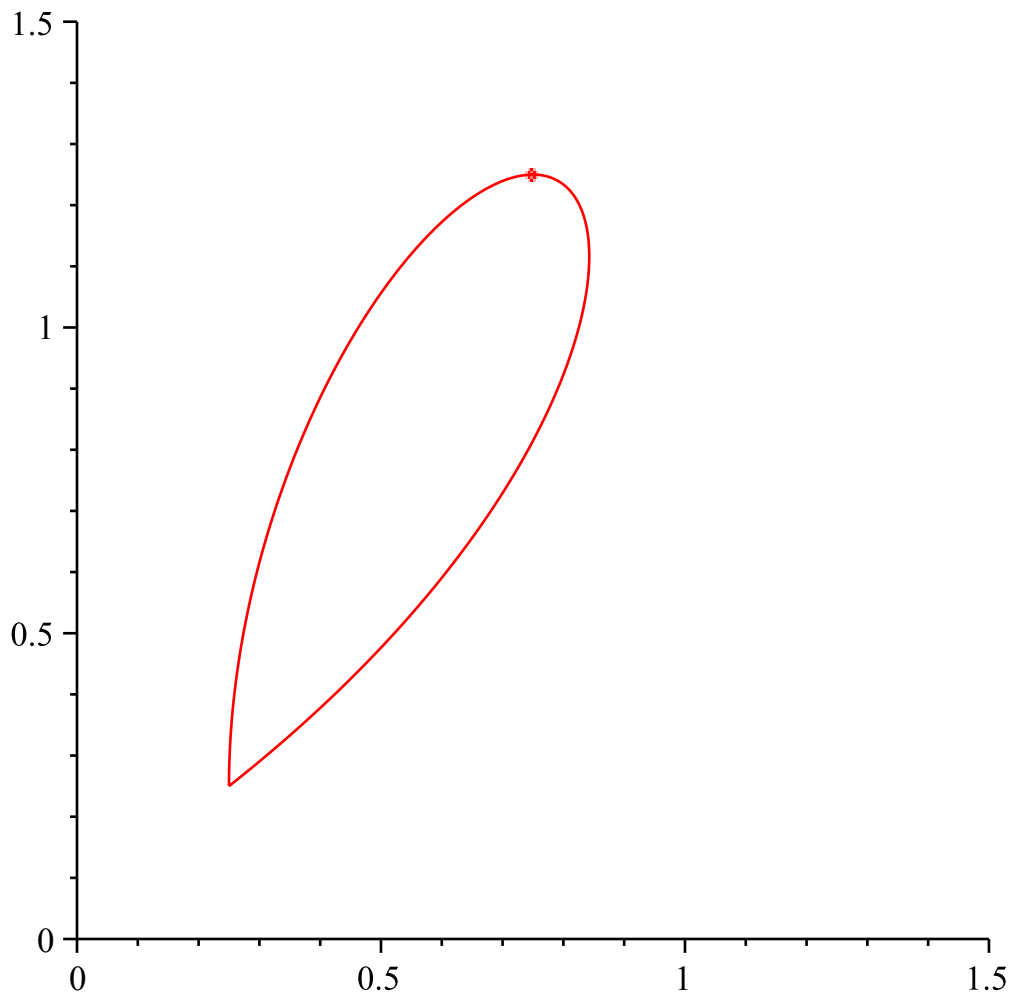
(5)

```
> P1:=plot([f,g,t=0..1],view=[0..1.5,0..1.5]):
```

```
> P2:=plot([[3/4,5/4]],style=point):
```

```
> with(plots):
```

```
> display(P1,P2);
```



```
> x0:=subs (t=1/2, f) ;
  y0:=subs (t=1/2, g) ;
```

$$x0 := \frac{3}{4}$$

$$y0 := \frac{1}{4} + \sin\left(\frac{1}{2} \pi\right) \quad (6)$$

```
> simplify(y0) ;
```

$$\frac{5}{4} \quad (7)$$

```
> m:=subs (t=1/2, dg/df) ;
```

$$m := \cos\left(\frac{1}{2} \pi\right) \pi \quad (8)$$

```
> simplify(m) ;
```

$$0 \quad (9)$$

```
> series (exp (x^2) , x=0, 6) ;
```

$$1 + x^2 + \frac{1}{2} x^4 + O(x^6) \quad (10)$$

```
>
```