

```
> restart;
```

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> #Maple Solutions to Honors Calculus Math 182 Quiz 2
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```
> #PROBLEM 1
```

```
> Q1:=3*x^2;
```

$$Q1 := 3x^2$$

```
> int(Q1,x);
```

$$x^3$$

```
> #so obviously choice (A) is okay. Now check the other choices:
```

```
> Q1b:=x^3-7;
```

```
Q1c:=(x-1)^3+3*x^2-3*x;
```

$$Q1b := x^3 - 7$$

$$Q1c := (x - 1)^3 + 3x^2 - 3x$$

```
> diff(Q1b,x);
```

$$3x^2$$

```
> temp:=diff(Q1c,x);
```

$$temp := 3(x - 1)^2 + 6x - 3$$

```
> simplify(temp);
```

$$3x^2$$

```
> #therefore the answer is (D) all of the above.
```

```
> #PROBLEM 2
```

```
> Q2:=2*sin(2*x);
```

$$Q2 := 2 \sin(2x)$$

```
> int(Q2,x);
```

$$-\cos(2x)$$

```
> #This doesn't appear on the list, but rules out choices (B), (C) and (D).
```

```
> #By process of elimination (A) must be correct. Check to be sure.
```

```
> Q2a:=sin(x)^2-cos(x)^2;
```

$$Q2a := \sin(x)^2 - \cos(x)^2$$

```
> temp:=diff(Q2a,x);
```

$$temp := 4 \sin(x) \cos(x)$$

```
> simplify(Q2-temp);
```

$$0$$

> #since the difference is 0 then (A) is an antiderivative.

> #PROBLEM 3

> Q3:=log(1/(x^2+2*x+1));

$$Q3 := \ln\left(\frac{1}{x^2 + 2x + 1}\right)$$

> temp:=int(Q3,x);

$$temp := \ln\left(\frac{1}{(x+1)^2}\right) (x+1) + 2x + 2$$

> factor(temp);

$$\left(\ln\left(\frac{1}{(x+1)^2}\right) + 2\right) (x+1)$$

> #This is not on the list but is close to all of them.

#At this point it is probably easiest to find the correct choice by further simplifications

#done by hand. Namely, $\log(1/(x+1)^2) = -2\log(\text{abs}(x+1))$ indicates the correct choice is (C).

> #PROBLEM 4

> Q4:=1/sqrt(4+x^2);

$$Q4 := \frac{1}{\sqrt{4 + x^2}}$$

> int(Q4,x);

$$\text{arcsinh}\left(\frac{1}{2}x\right)$$

> #Note that asinh and arcsinh are the same function so (C) contains an antiderivative.

#Given choices (D) and (E) some additional work is needed.

> Q4a:=log(x+sqrt(x^2+4));

$$Q4a := \ln(x + \sqrt{4 + x^2})$$

> temp:=diff(Q4a,x);

$$temp := \frac{1 + \frac{x}{\sqrt{4 + x^2}}}{x + \sqrt{4 + x^2}}$$

```
> simplify(temp);
```

$$\frac{1}{\sqrt{4 + x^2}}$$

```
> #Therefore (A) is also an antiderivative. Obviously (B) is off by a  
#factor of 2 so the  
#correct choice is (D).
```

```
> #PROBLEM 5
```

```
> #By definition of the hyperbolic sine function the area given by A=t/2  
where sinh(t)=4/3.  
#Therefore the answer to part 5(ii)
```

```
> Q5i:=1/2*arcsinh(4/3);
```

$$Q5i := \frac{1}{2} \operatorname{arcsinh}\left(\frac{4}{3}\right)$$

```
> #The decimal approximation is obtained using evalf
```

```
> evalf(Q5i);
```

0.5493061440

```
> #The derivatives are surely easier to do by hand. But for completeness  
here they are with Maple.
```

```
> Q6i:=abs(sin(x))^3;
```

$$Q6i := |\sin(x)|^3$$

```
> temp:=diff(Q6i,x) assuming x::real;
```

$$\text{temp} := 3 |\sin(x)|^2 \operatorname{signum}(\sin(x)) \cos(x)$$

```
> simplify(temp);
```

$$3 |\sin(x)| \cos(x) \sin(x)$$

```
> Q6ii:=7*arctan(x^2);
```

$$Q6ii := 7 \arctan(x^2)$$

```
> diff(Q6ii,x);
```

$$\frac{14x}{1+x^4}$$

```
>
```