Honors Math 182 Bonus Quiz 11 Version A

The score on this quiz will be used to replace one score from among your homework or quiz scores, whichever provides greater benefit.

1. Find the following anitiderivates:

(i)
$$\int (\sin x)(\sin 2x) \, dx$$

(ii)
$$\int \frac{2x^2}{(x-1)(x+3)} \, dx$$

(iii)
$$\int x \ln(x^2 + 1) \, dx$$

2. Find the following limits:

(i)
$$\lim_{x \to 0} \frac{\sin x - x \cos x}{x^3}$$

(ii)
$$\lim_{x\to 0} \frac{\ln(1+x^2) - \arctan^2 x}{x^4}$$

(iii) Use either Newton's method, the Taylor theorem or continued fractions to obtain a sequence of rational numbers that converge to $\sqrt{5}$.