

```
> restart;
> t:=n->t0+n*h;
t := n ↦ t0 + n h (1)
```

```
> t(2);
t0 + 2 h (2)
```

```
> p:=x->f(t(n-1),ynm1)*(x-t(n))*(x-t(n+1))/((t(n-1)-t(n))*(t(n-1)-t(n+1)))
+f(t(n),yn)*(x-t(n-1))*(x-t(n+1))/((t(n)-t(n-1))*(t(n)-t(n+1)))
+f(t(n+1),ynp1)*(x-t(n-1))*(x-t(n))/((t(n+1)-t(n-1))*(t(n+1)-t(n)));
```

```
p := x ↦ 
$$\frac{f(t(n-1), ynm1) (x-t(n)) (x-t(n+1))}{(t(n-1)-t(n)) (t(n-1)-t(n+1))} + \frac{f(t(n), yn) (x-t(n-1)) (x-t(n+1))}{(t(n)-t(n-1)) (t(n)-t(n+1))} + \frac{f(t(n+1), ynp1) (x-t(n-1)) (x-t(n))}{(t(n+1)-t(n-1)) (t(n+1)-t(n))}$$
 (3)
```

```
> simplify(p(x));

$$\frac{1}{2 h^2} ((n h + t0 - x) ((n + 1) h - x + t0) f(t0 + (n - 1) h, ynm1) + ((n - 1) h - x + t0) ((n h + t0 - x) f(n h + h + t0, ynp1) - 2 f(n h + t0, yn) ((n + 1) h - x + t0)))$$
 (4)
```

```
> sort(simplify(int(p(x),x=t(n)..t(n+1))));

$$\frac{(f((n-1) h + t0, ynm1) - 8 f(n h + t0, yn) - 5 f(n h + h + t0, ynp1)) h}{12}$$
 (5)
```